

# Fumbling Towards Inquiry: Starting Strong in Problem- Based Learning

(So everyone's  
happier.)



## NCTM Annual Conference 2016

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[emergentmath.com](http://emergentmath.com)



*Geoff Krall*

*Fumbling Towards  
Inquiry*



# Objectives

Experience part of a Problem-Based Learning Lesson

Discuss five design principles and carving a path toward inquiry

Identify first/next steps as a teacher

Student generated  
questions

Instruction

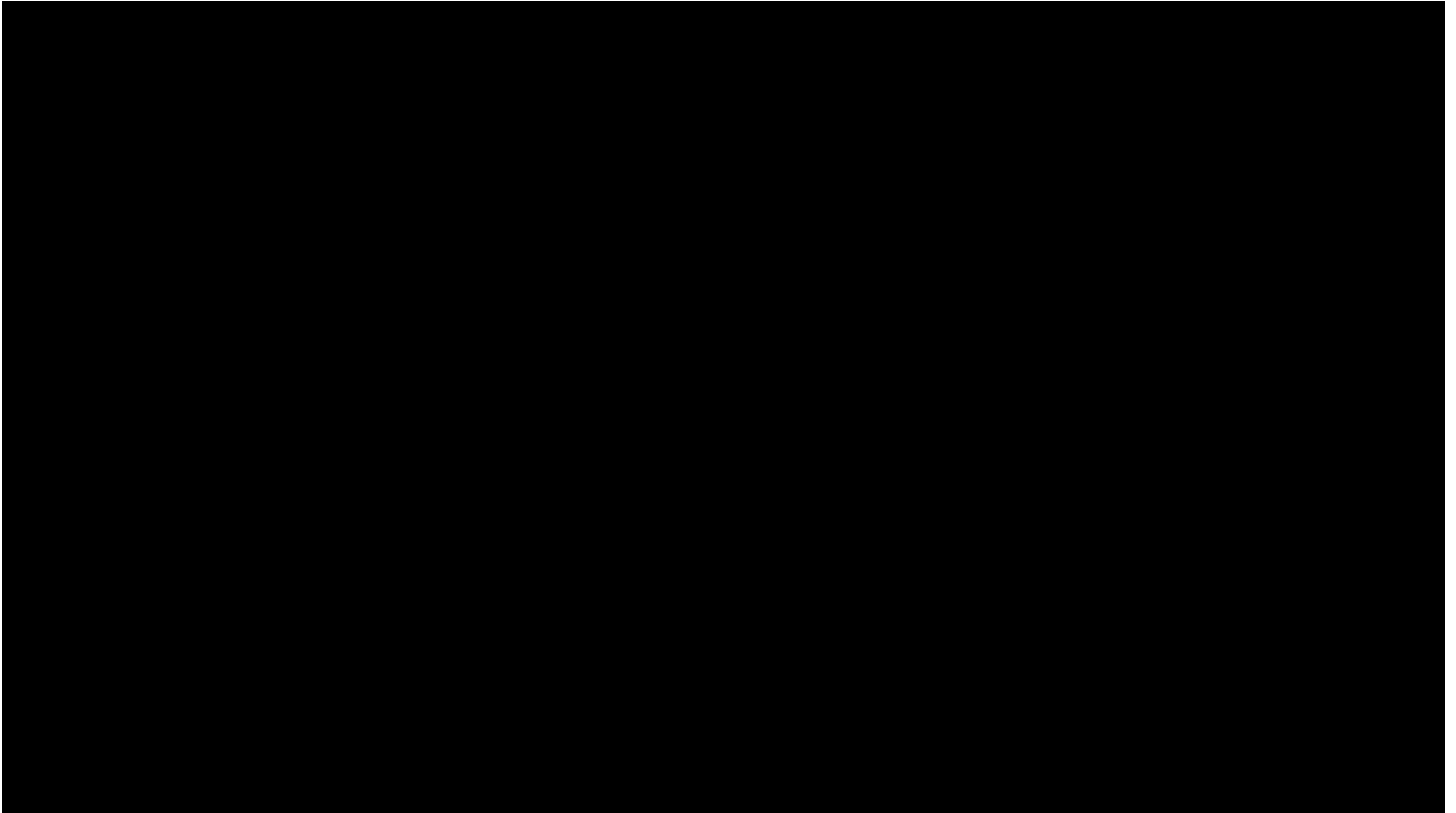
Problem(s)

Content Delivery Content Delivery

Research clearly suggests that problem solving should not be taught as a separate topic in the mathematics curriculum. In fact, research tells us that teaching students to use general problem-solving strategies has little effect on their success as problem solvers. Thus, problem solving must be taught as an integral part of mathematics learning, and it requires a significant commitment in the curriculum at every grade level and in every mathematical topic. - NCTM

## Research Brief on Problem Solving

# Entry Event: The Race





## Problem Solving Framework

### Define the Problem

What is the problem about? What is it asking you to do?

### Analyze the Problem

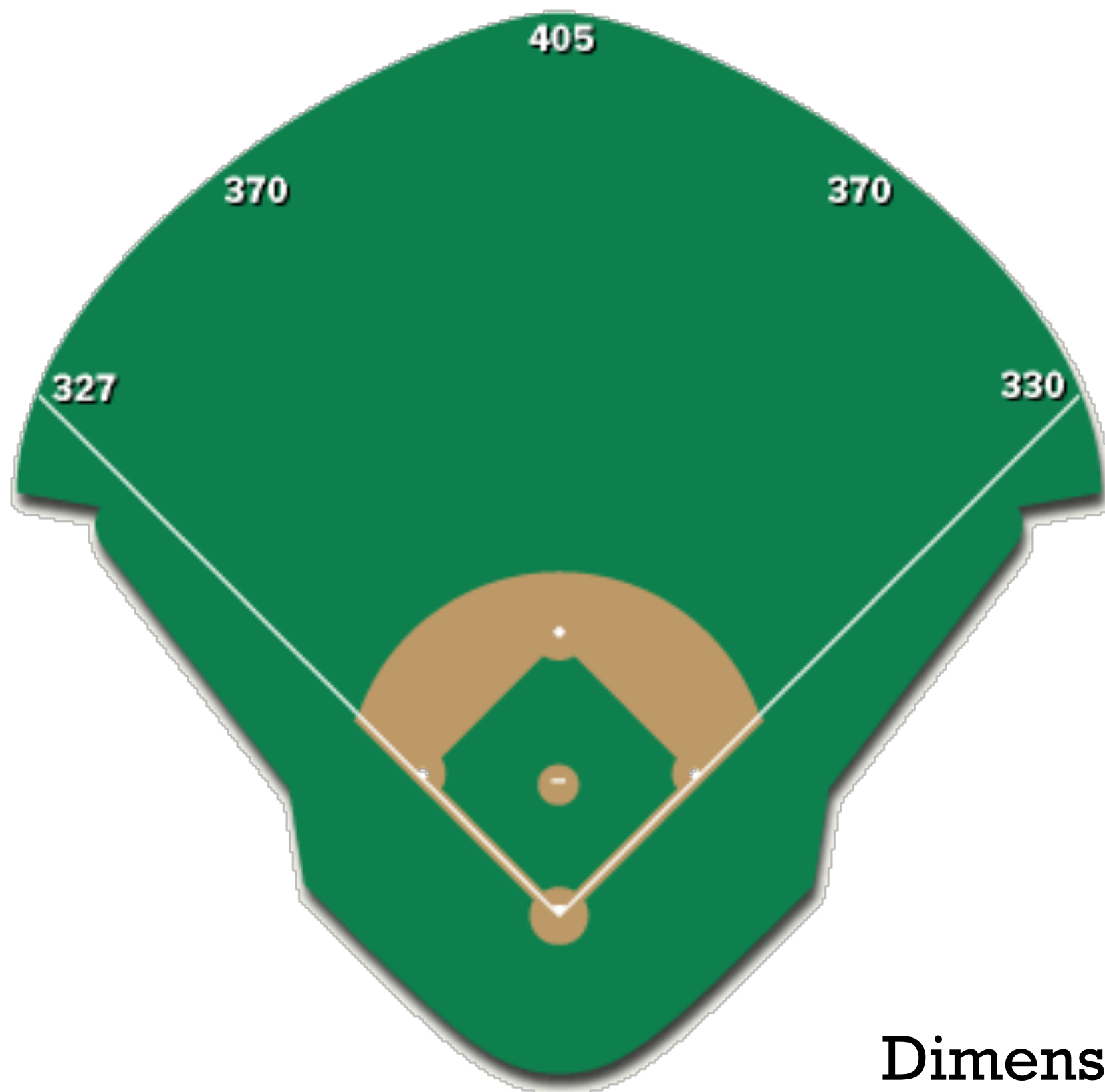
What do you **know/notice** from the problem scenario or previous lessons that can help solve the problem?

What concepts or information do you **need to know** in order to solve the problem?

### Brainstorm Strategies for Solving the Problem

What strategies might you use to solve the problem? How will you start the problem?





Dimensions of  
Qualcomm Field

comcast  
SPORTSNET

00:00:00:00





0.0 feet

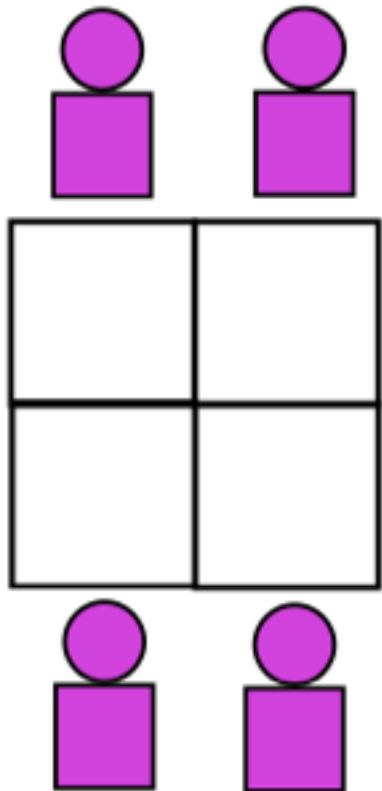
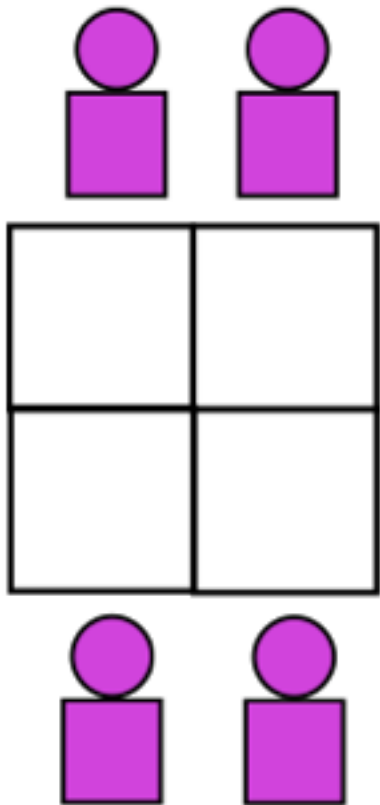
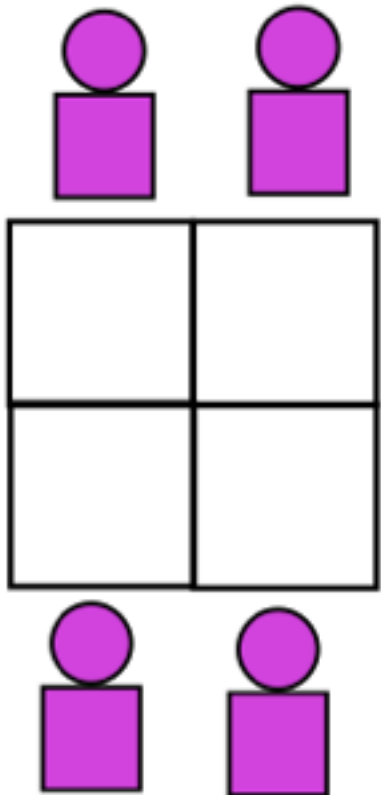
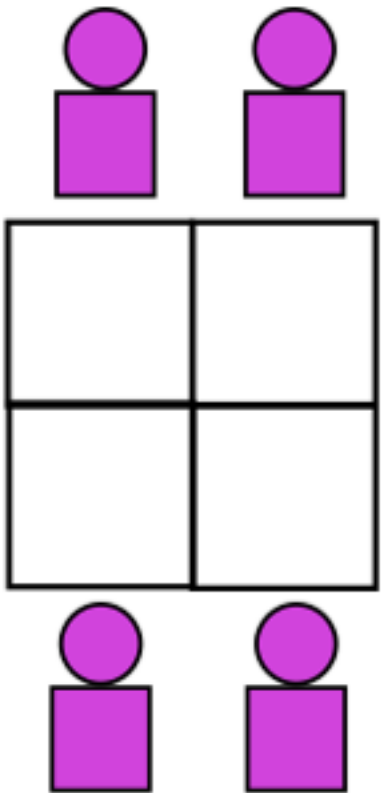
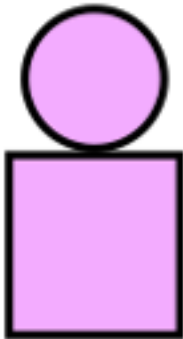
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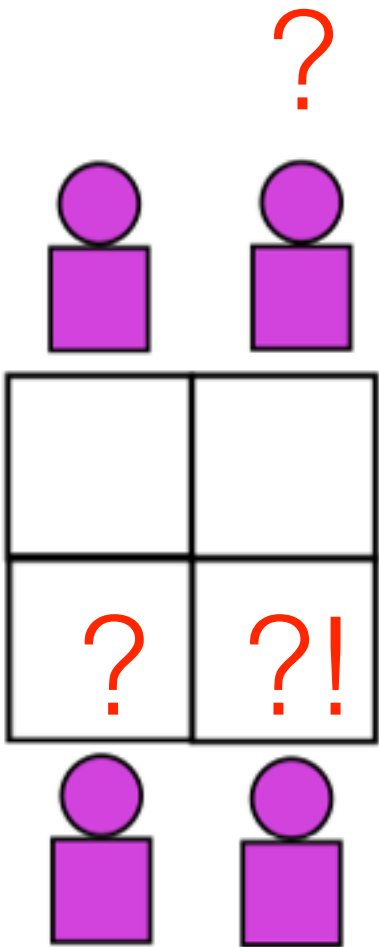
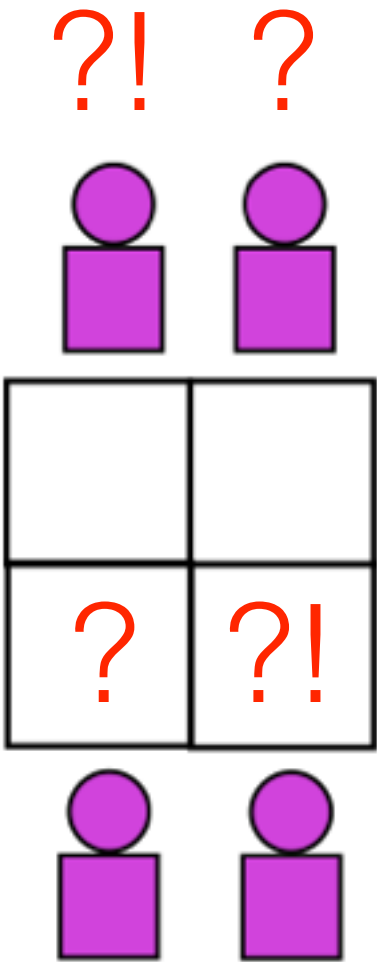
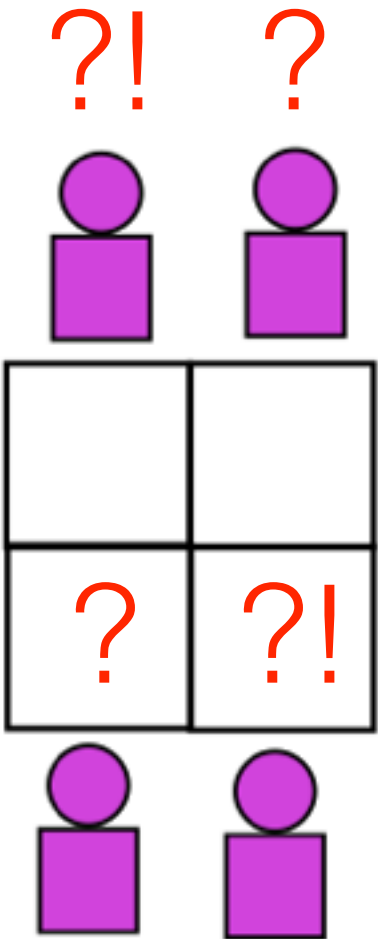
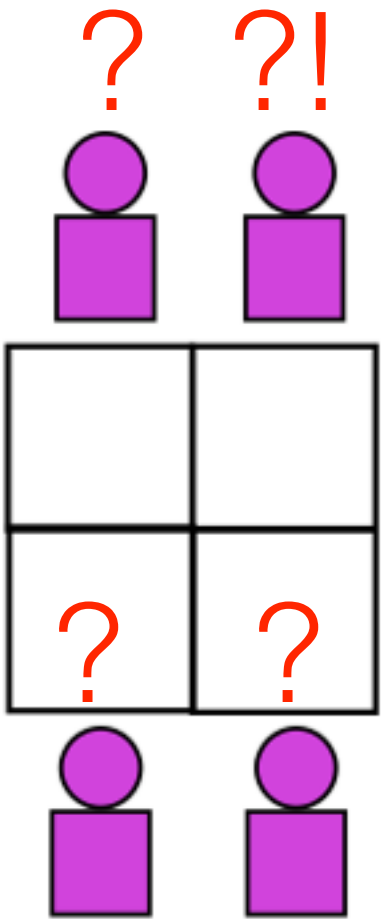
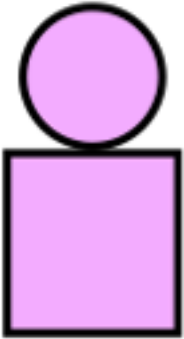




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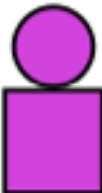
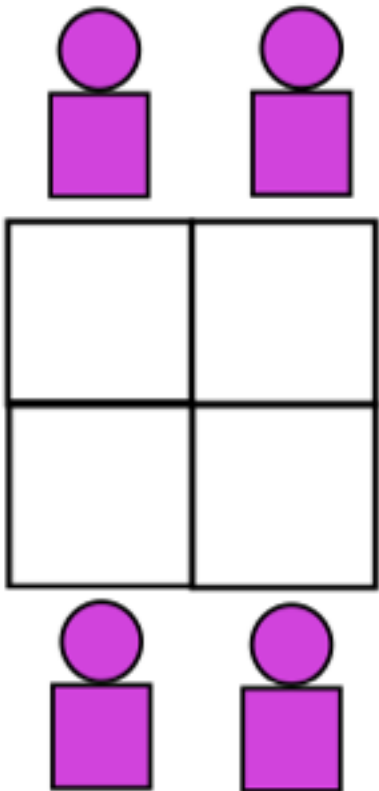
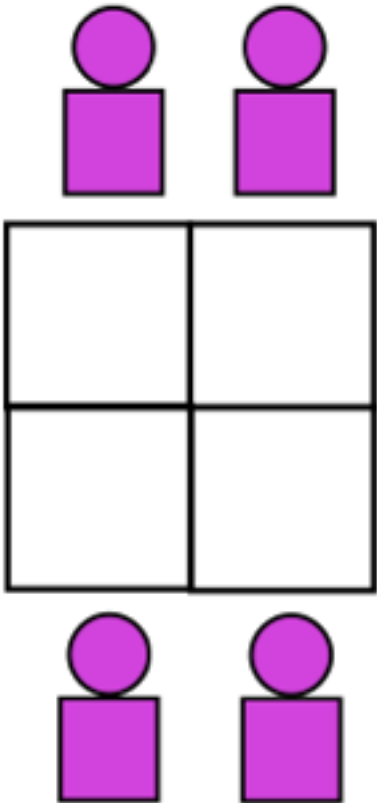
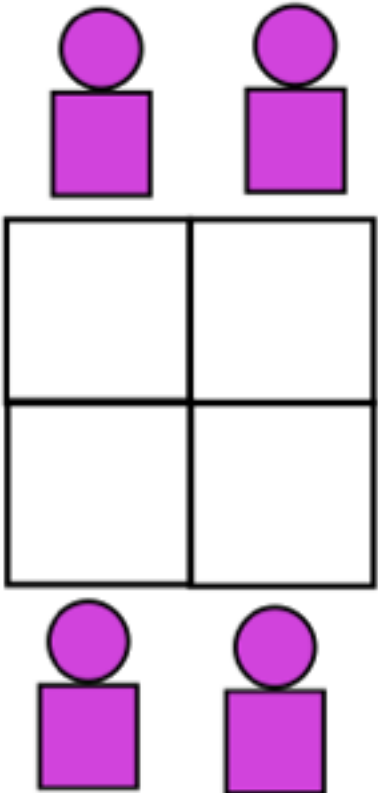
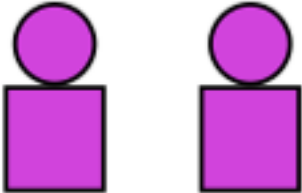
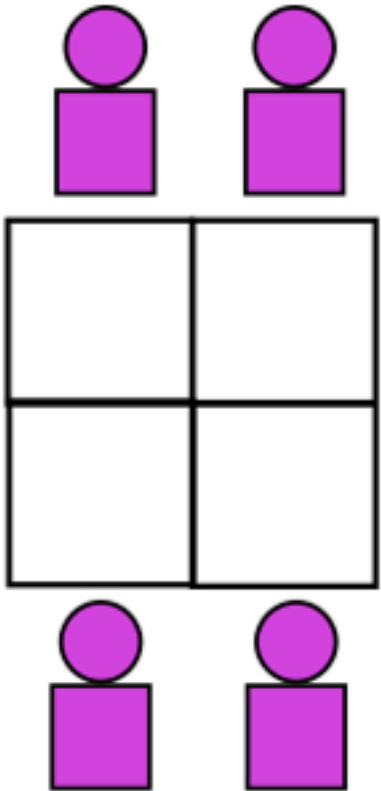
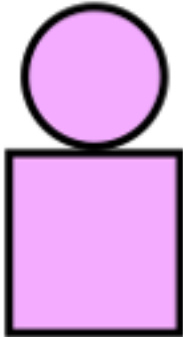
0.0 feet







$y=mx+b$





# My 2-day Agenda

MONDAY	TUESDAY
<p>Warm Up</p> <p>Show Entry Event (Squirrel Race Guy)</p> <p>Solicit Knows/Need to Knows</p> <p>Reveal crucial info based on NTKs</p> <p>Workshop on Pythagorean Theorem (if necessary)</p> <p>Revisit Knows/Need to Knows</p> <p>Exit Ticket</p>	<p>Warm Up</p> <p>Lesson: Systems of Equations Revisit Need-to-Knows</p> <p>Workshop (if necessary): Writing an equation based on a scenario</p> <p>Student work time: Equation, Graphs, Systems</p> <p>Present solutions in a gallery walk</p> <p>Exit Ticket</p>

[An] important barrier to meaningful problem solving experiences is that **teachers often remove the challenges of a mathematical task by taking over the thinking** and reasoning and telling students how to solve the problem. - NCTM Research Brief on Problem Solving

# Five Design Principles to develop a Problem-Based Learning classroom

## Design Principle #1: Notch some early wins

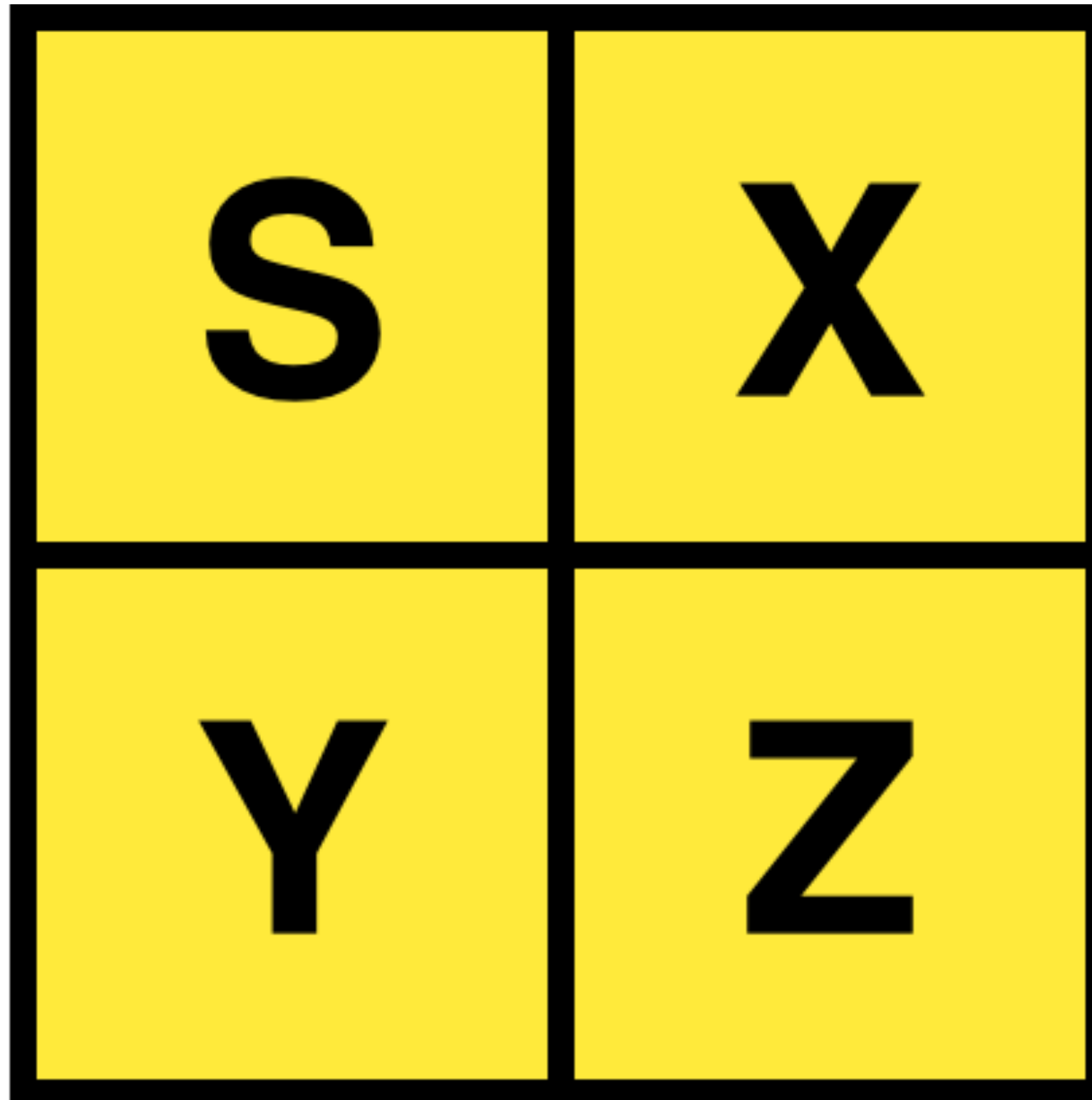
Get kids talking mathematically

Get kids sharing ideas with one another

Start with short 10-20 minute math explorations

**Get kids thinking of themselves as mathematicians**

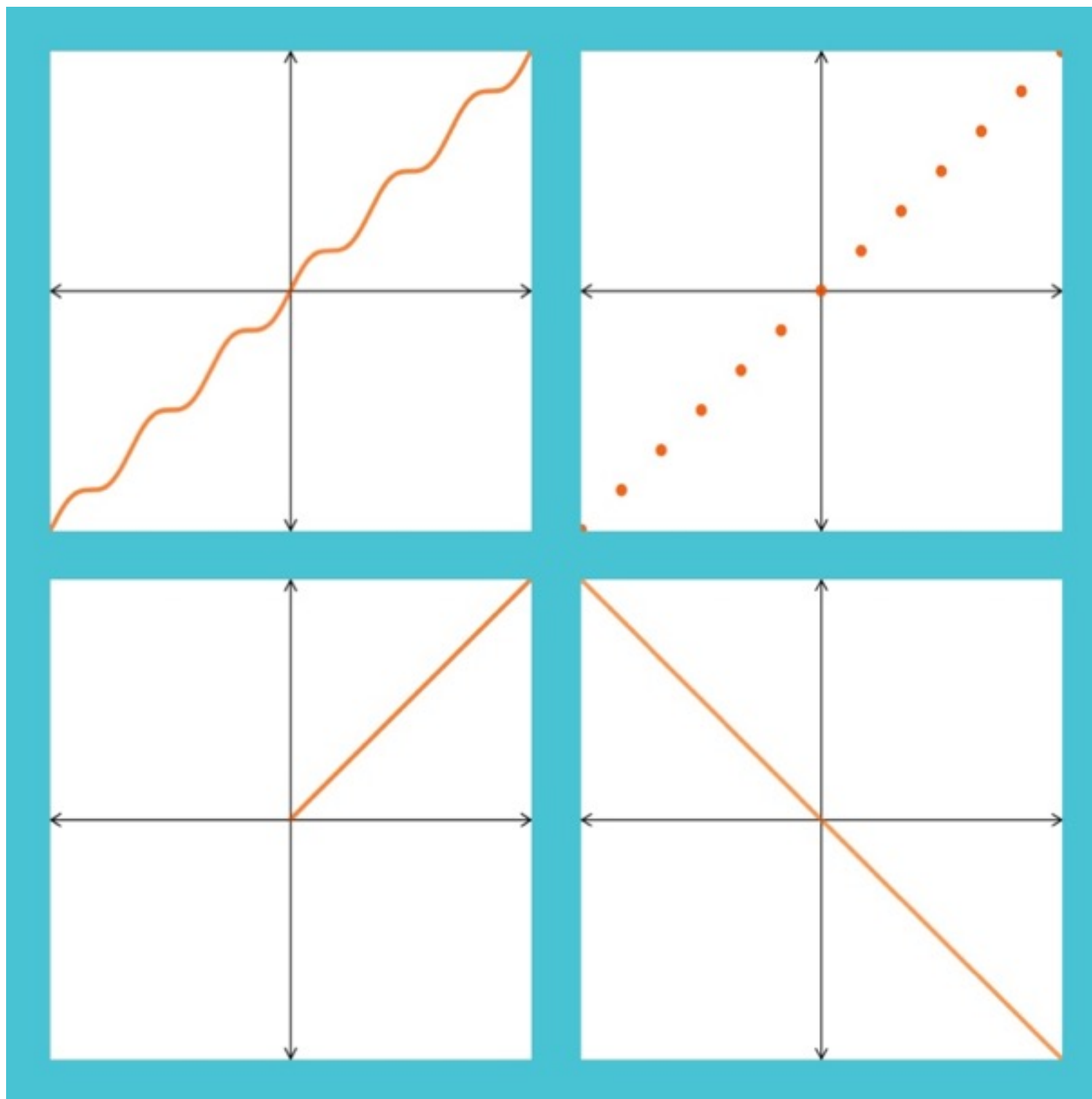
**Which One Doesn't Belong?**



**Which One Doesn't Belong?**

121	16
9	73

# Which One Doesn't Belong?





# Estimation

How many **cheeseballs** will fit on the *large* plate?



**Make an estimate.**

\* Required

**What's too LOW? \***

**What's too HIGH? \***

**Your estimate. \***

**Your reasoning. \***

Do better than "I guessed." Try "I noticed"

**Your name.**

[estimation180.com](http://estimation180.com) - Andrew Stadel @mr\_stadel

[Home](#)[Kinder ▾](#)[Grade 1 ▾](#)[Grade 2 ▾](#)[Grade 3 ▾](#)[Grade 4 ▾](#)[Grade 5 ▾](#)[Grade 6 ▾](#)[Grade 7 ▾](#)

[Home](#) > [Grade 5](#) > Subtracting Mixed Numbers

## SUBTRACTING MIXED NUMBERS

Directions: Using the whole numbers from 1 to 9, at most one time each, find three different mixed numbers that will make the equation true. You may reuse the same numbers for each of the three numbers.

$$5\frac{4}{5} - \boxed{\phantom{00}}\frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} = 3\frac{1}{20}$$

Hint



Design Principle #1: Notch some early wins

Design Principle #2: Provide an iterative  
framework

Get kids talking mathematically

Get kids sharing ideas

Start with short 10-20 minute math explorations

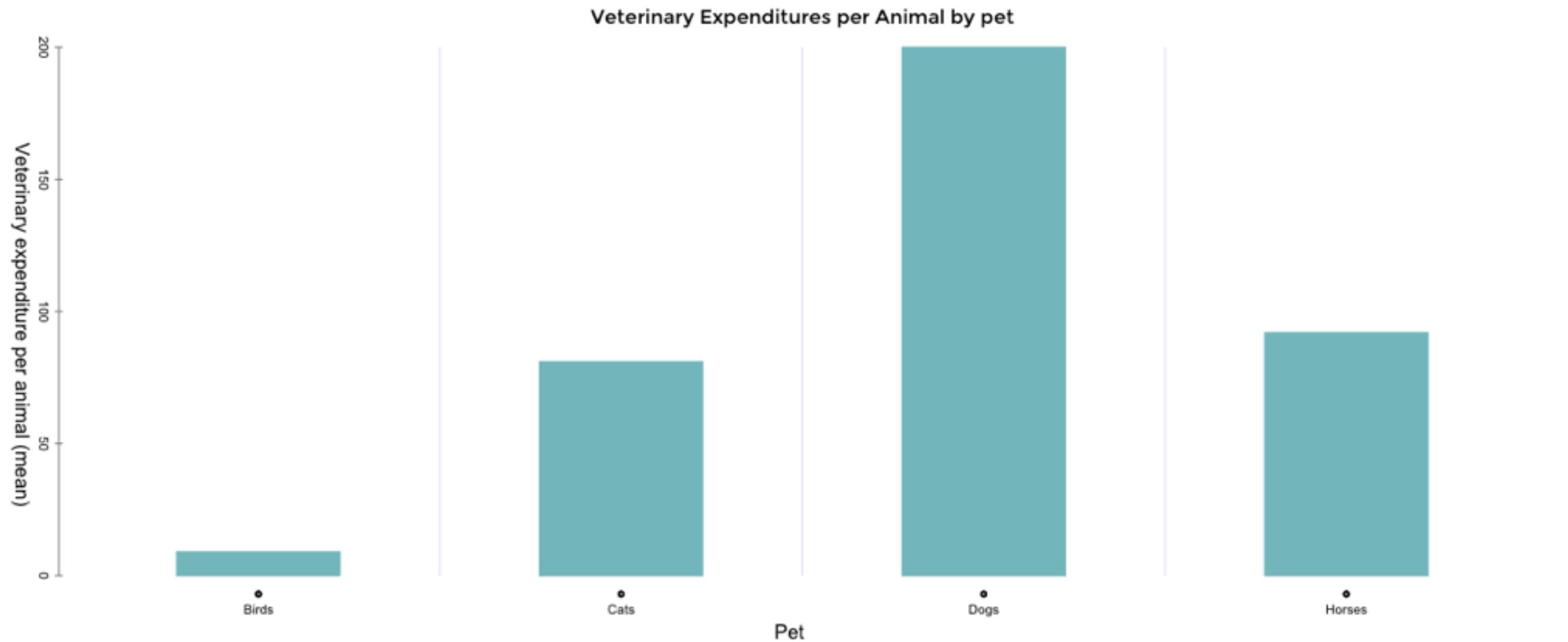
**Get kids thinking of themselves as mathematicians**

# Know / Need-to-Know Process

## Problem Solving Framework

Define the Problem	
What is the problem about? What is it asking you to do?	
Analyze the Problem	
What do you <b>know/notice</b> from the problem scenario or previous lessons that can help solve the problem?	What concepts or information do you <b>need to know</b> in order to solve the problem?
Brainstorm Strategies for Solving the Problem	
What strategies might you use to solve the problem? How will you start the problem?	

# Notice and Wonder

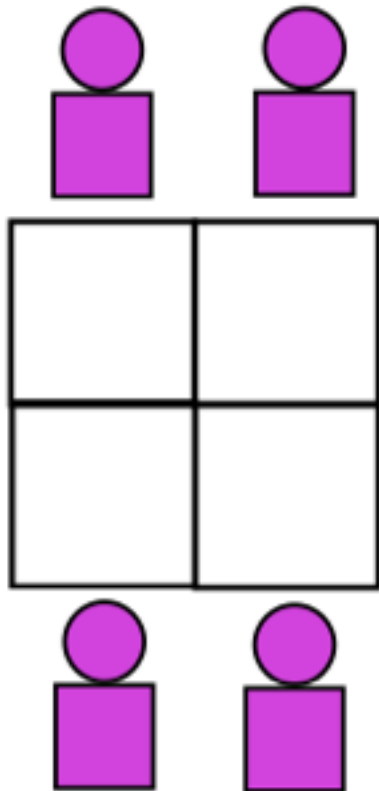
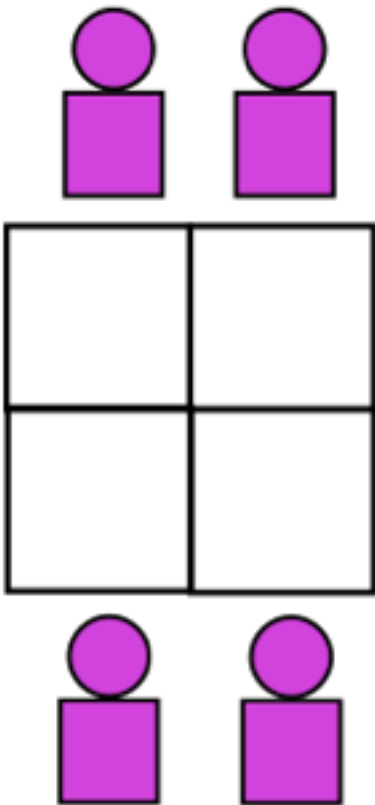
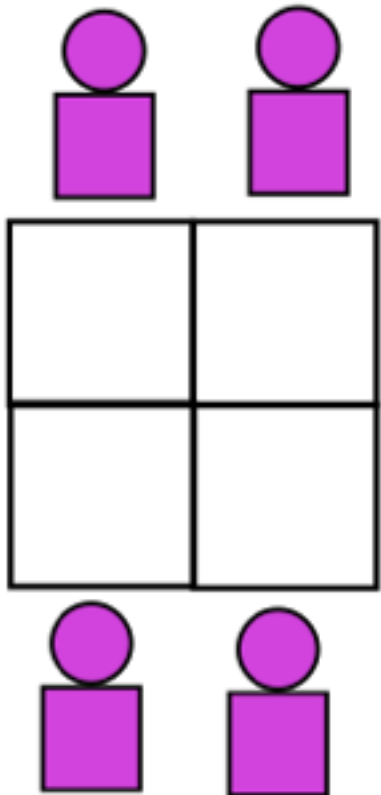
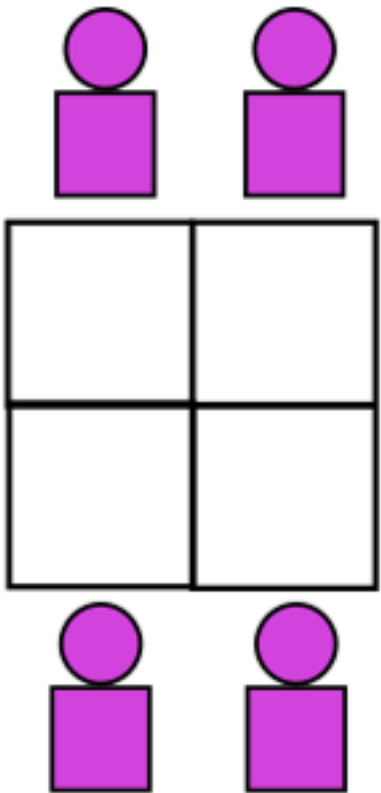
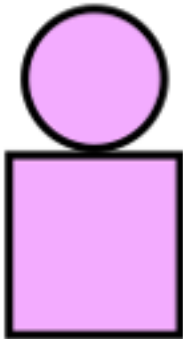


Design Principle #1: Notch some early wins

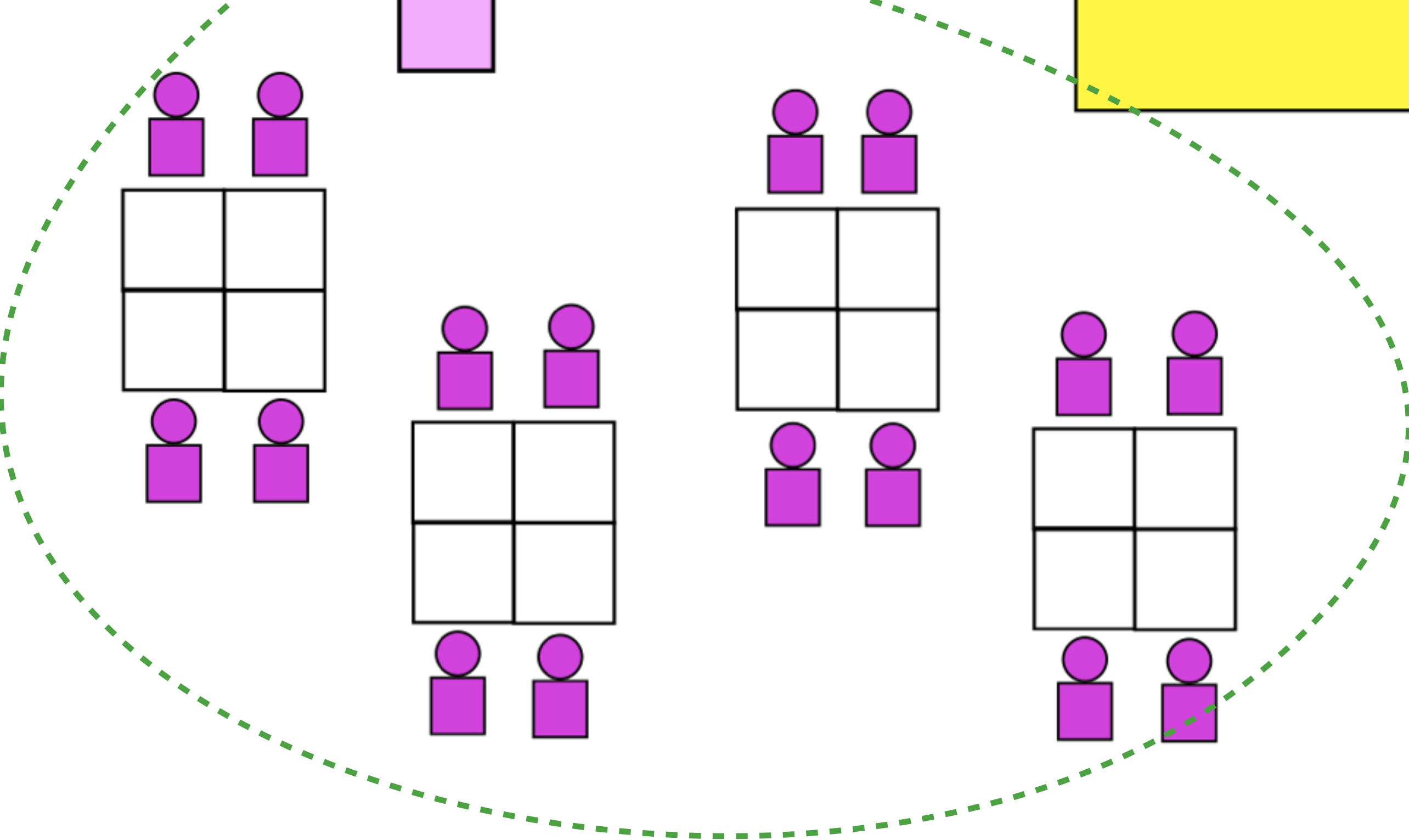
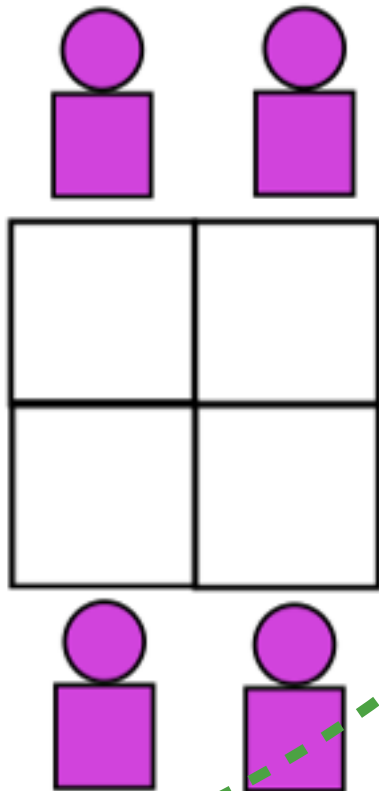
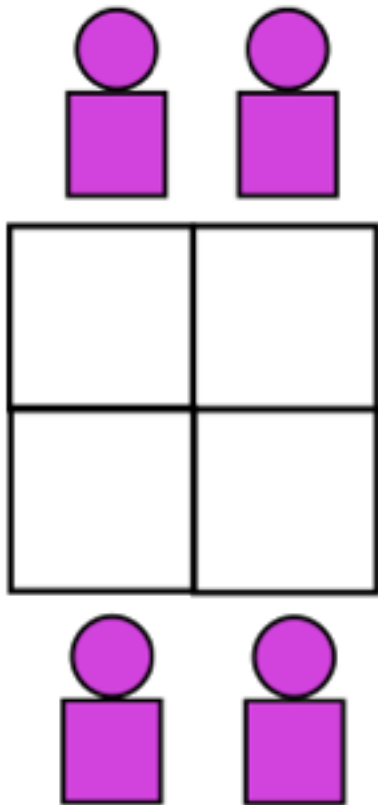
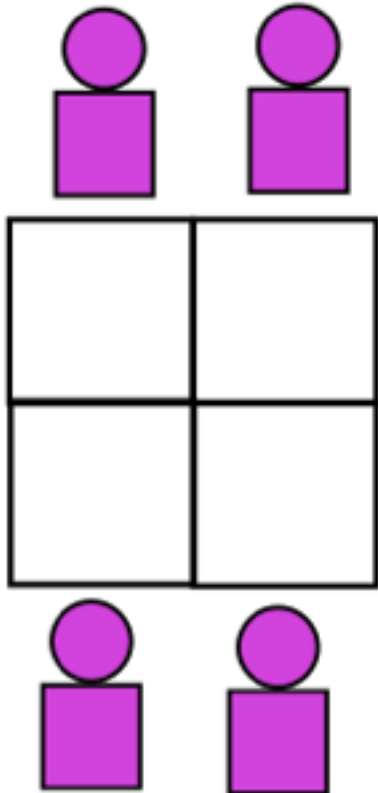
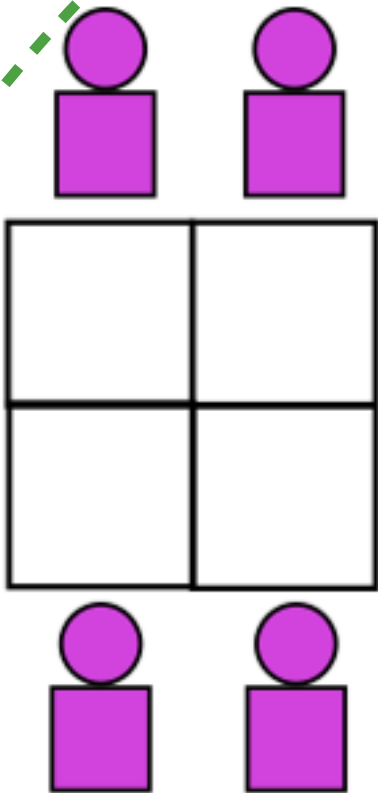
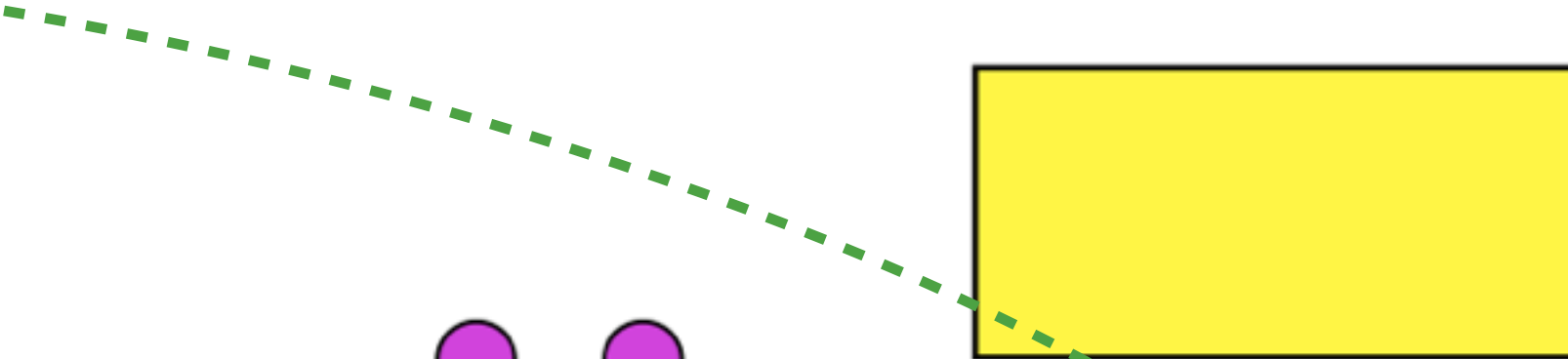
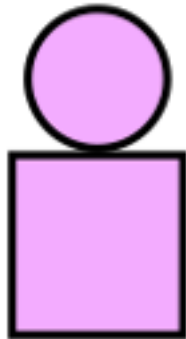
Design Principle #2: Provide an iterative framework

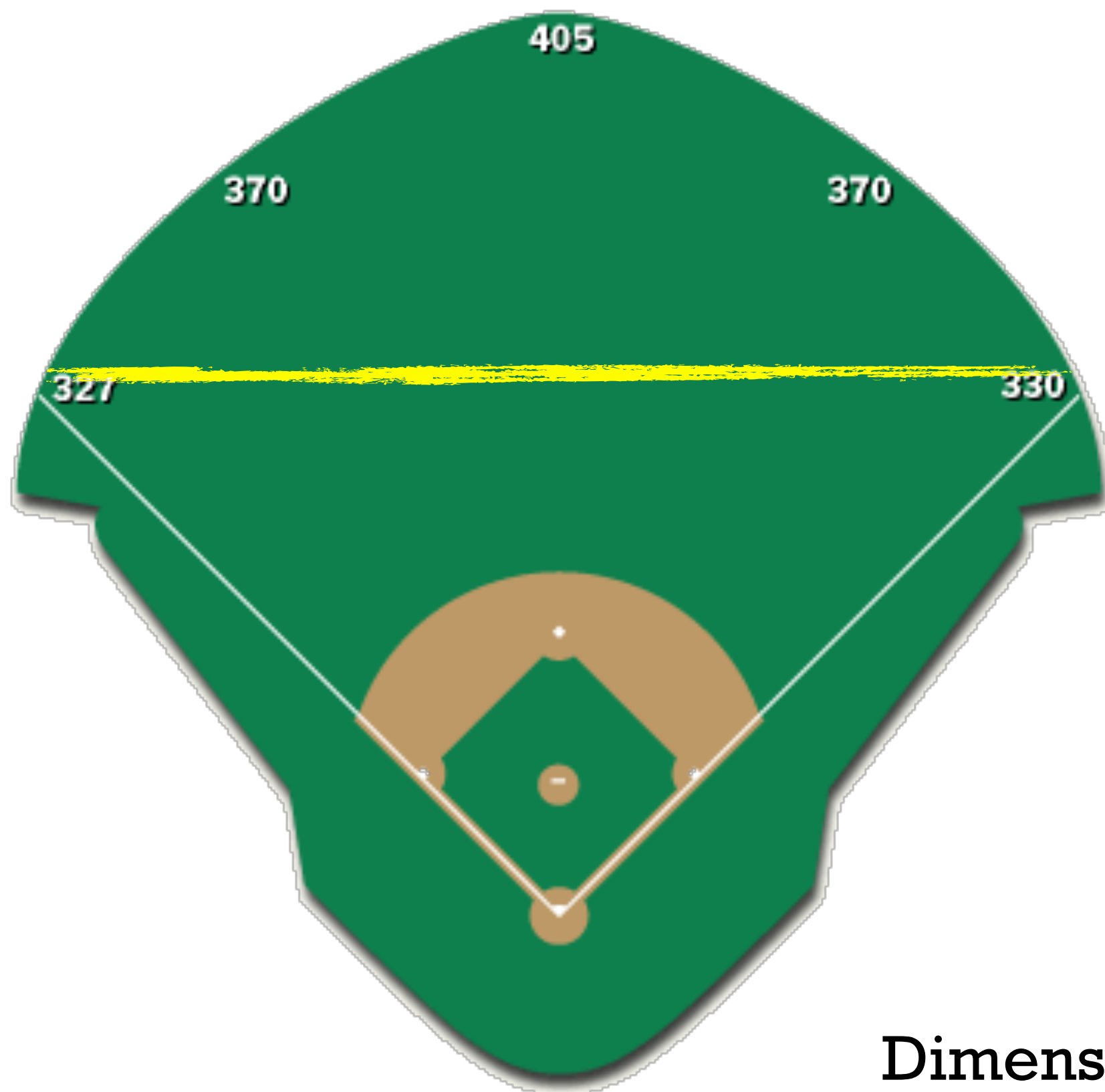
Design Principle #3: Tasks support targeted instruction & group-mate expertise



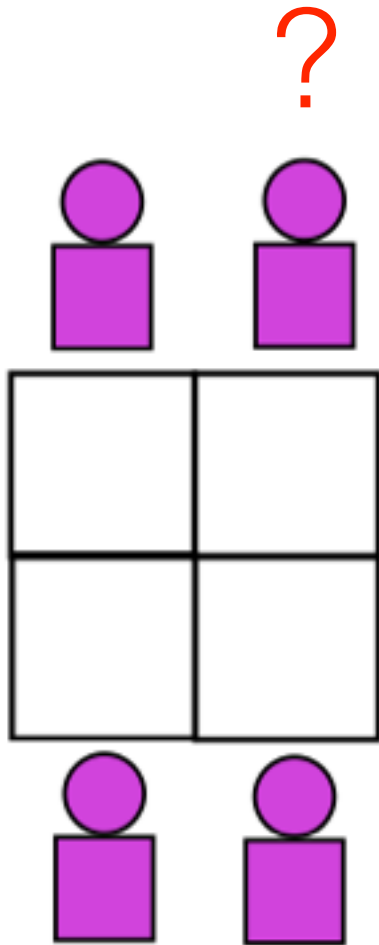
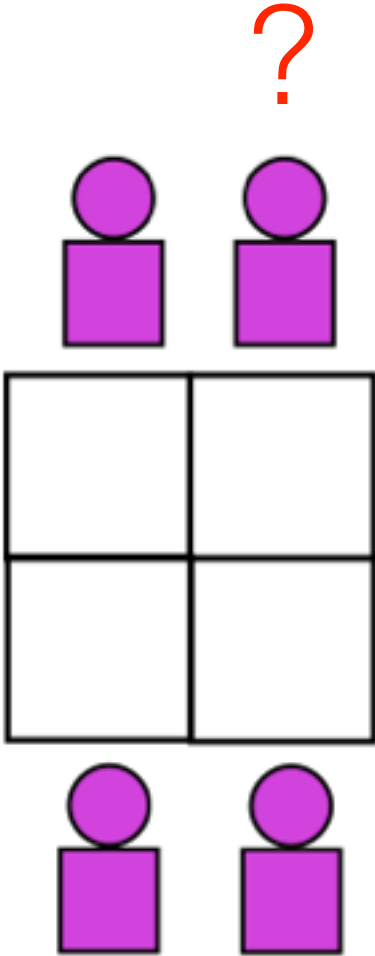
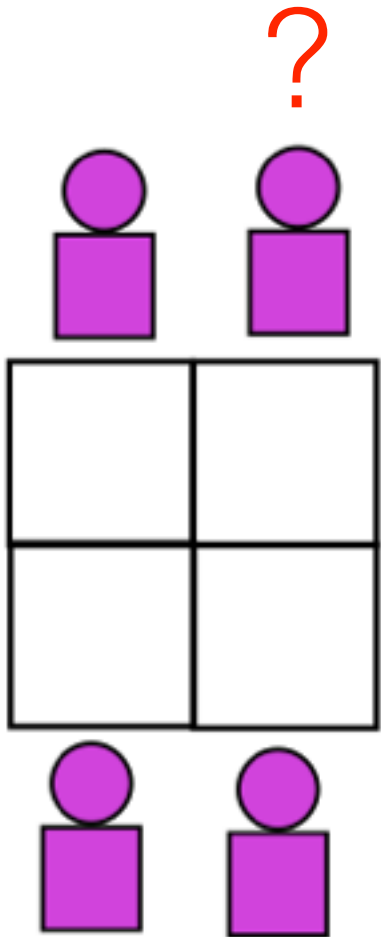
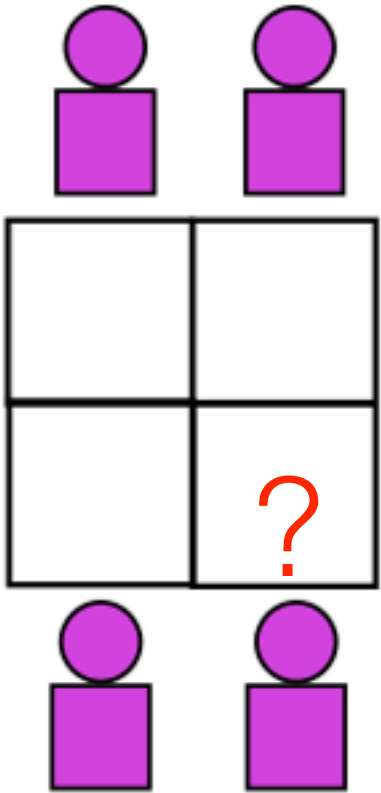
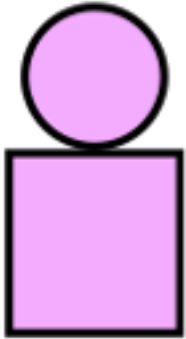




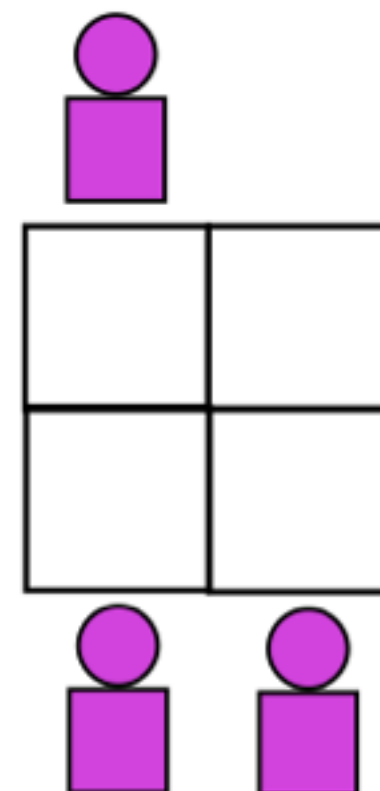
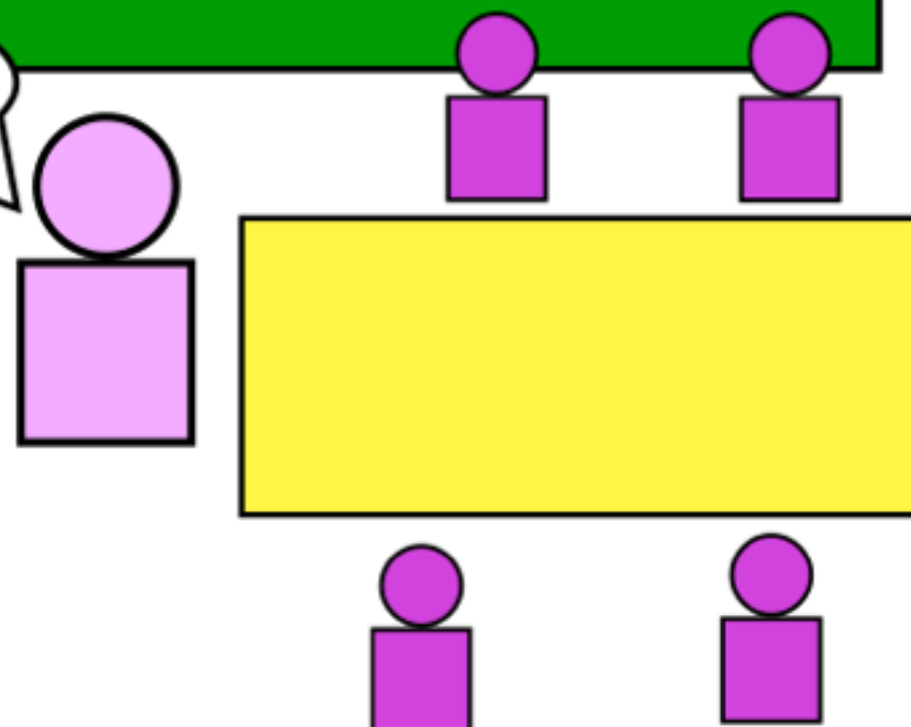
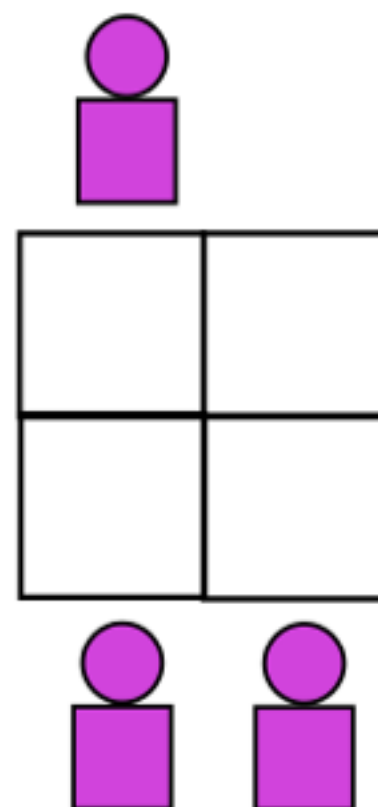
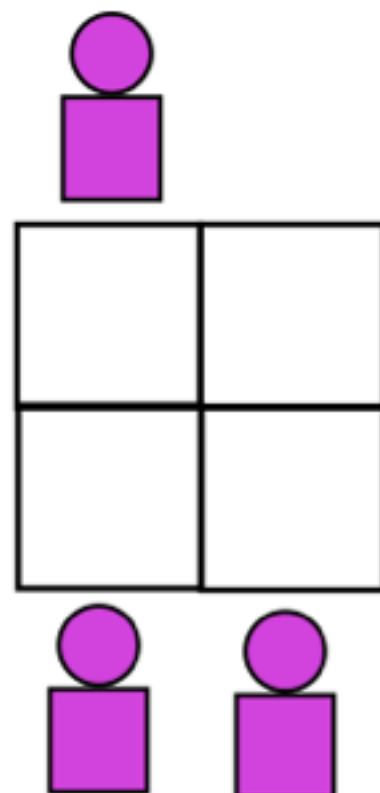
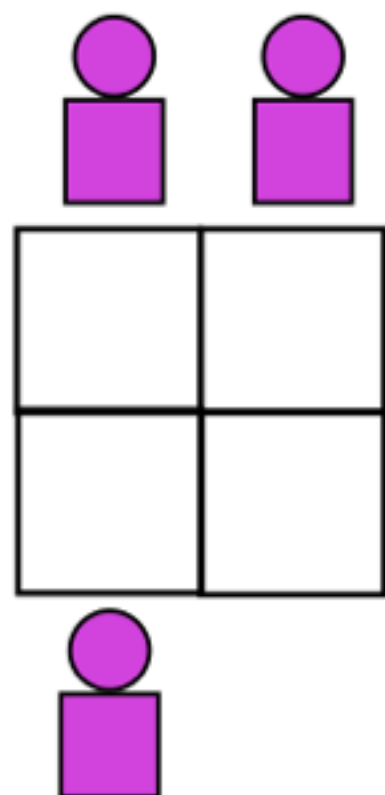


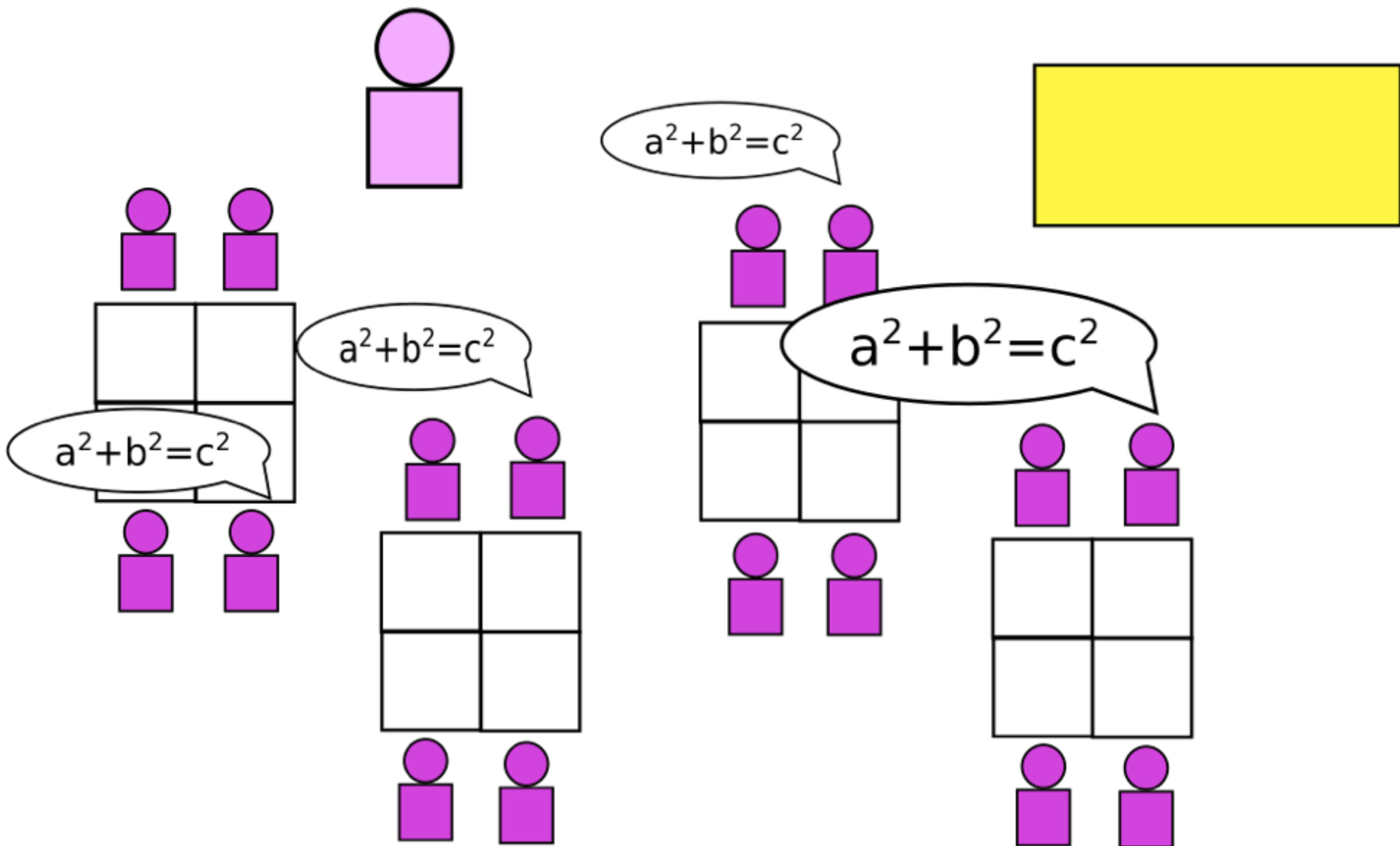


Dimensions of  
Qualcomm Field



$a^2 + b^2 = c^2$





Design Principle #1: Notch some early wins

Design Principle #2: Provide an iterative framework

Design Principle #3: Tasks support targeted instruction & group mate expertise

Design Principle #4: Start slowly and steadily

MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY



= Structured teacher-centric environment



= Inquiry



MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY





= Structured teacher-centric environment



= Inquiry






MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY

 = Structured teacher-centric environment

 = Inquiry

WHICH ONE DOESN'T BELONG?

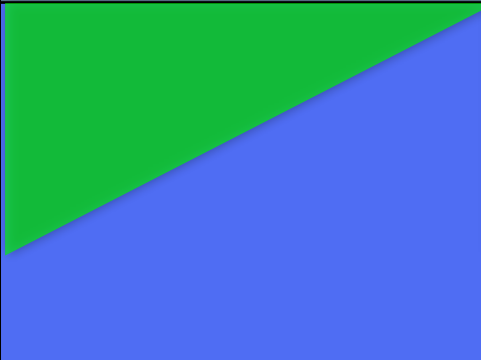
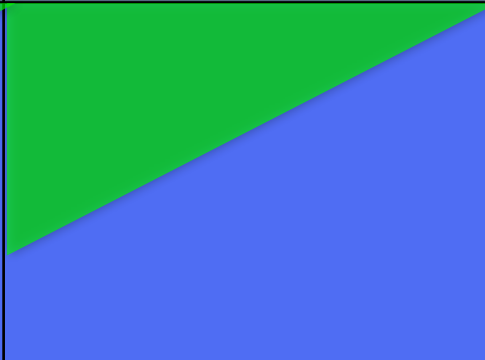

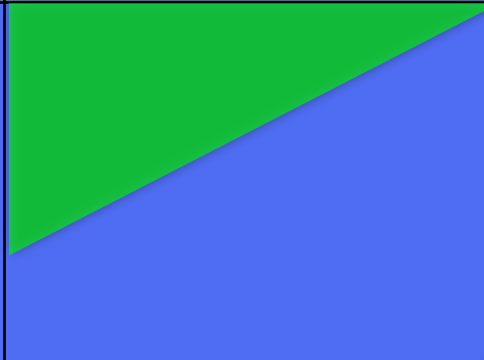
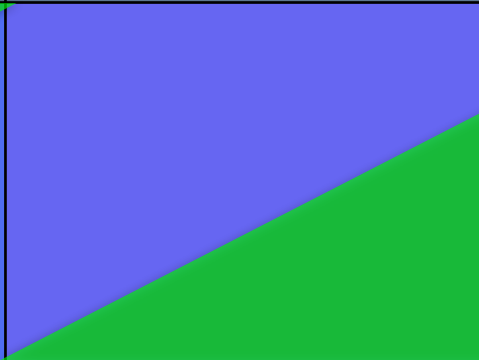
ESTIMATION180

MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY
				

ESTIMATION180

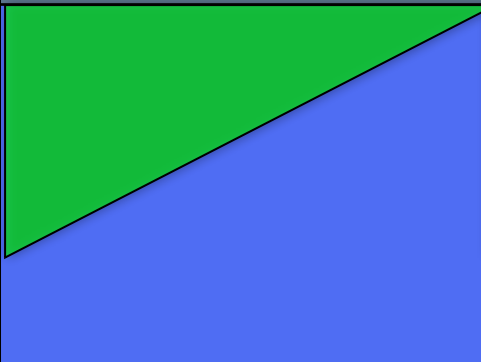
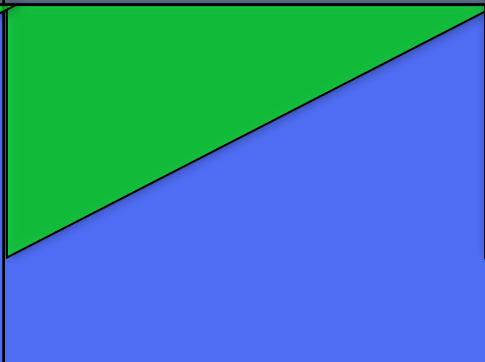
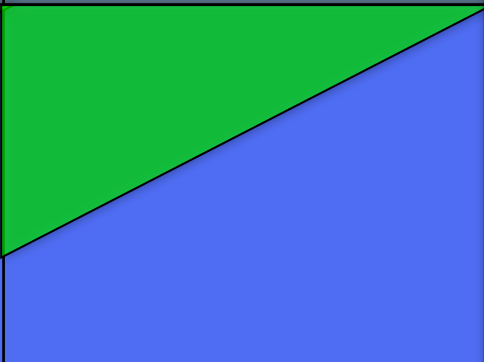


WHICH ONE DOESN'T BELONG?

ESTIMATION180

MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY
				

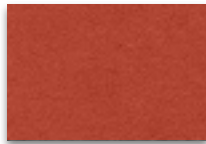
OPEN MIDDLE  
DOK - LEVEL 2/3

PROBLEM-BASED LEARNING  
TASK & LESSON

MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY
				

3-ACT MATH

MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY
Light Green	Light Green / Blue	Blue	Light Green	Brown
Blue	Light Green	Blue	Blue	Light Green
Blue	Brown	Light Green / Blue	Brown	Light Green / Brown
Brown	Brown	Brown	Light Green / Blue	Brown
Brown	Brown	Brown	Light Green	Light Green



=

Benchmarking / state testing

**To help students become successful problem solvers, teachers must accept that students' problem-solving abilities often develop slowly, thereby requiring long-term, sustained attention to making problem solving an integral part of the mathematics program. - NCTM Research Brief on Problem Solving**

Design Principle #1: Notch some early wins

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Design Principle #4: Start slowly and steadily

Design Principle #5: Don't go it alone



**Partner Up**  
Colleagues  
Twitter - “The Math Twitter Blogosphere”

## Select

Find 2-3 tasks that will produce rich student-thinking artifacts:  
Poster paper  
Disciplinary writing

## Implement

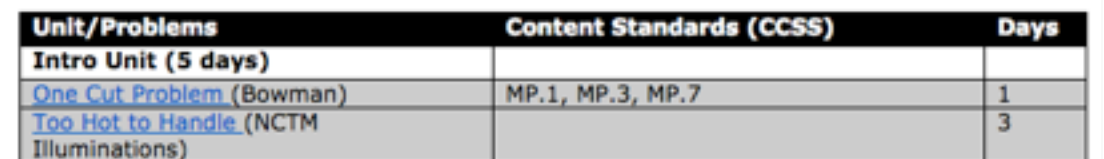
Sometime within the next couple weeks

## Debrief

How did it go?  
What kind of work did it produce (LASW protocols)?  
What became clear about student understanding of the concept? What remains unclear?

illustrativemathematics.org

**emergentmath.com**



UNIT: Exponential Functions	N-RN.1,2,3, A-SSE.3,4*, F-IF.3,7e,8b, F-BF.2,4a, F-LE.1a,1b,1c,2,3,4,5	25
<a href="#">Wolfram Alpha Real Numbers Investigation</a> (Fred)	N-RN.1,2,3	2
<a href="#">Lost in Recursion</a> (Paul)	F-IF.3	1
<a href="#">National Debt and Wars</a> (NCTM Illuminations)	F-IF.8c	2
<a href="#">Exponential Growth and Credit Cards</a>	F-IF.8c	1

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